

Monday Nov. 26
Lecture 22

Reverse of

tail

()
input →



reverse(bcdefgh)

output →

hgfedcb (a)

()
input →

abcdefgh (h)

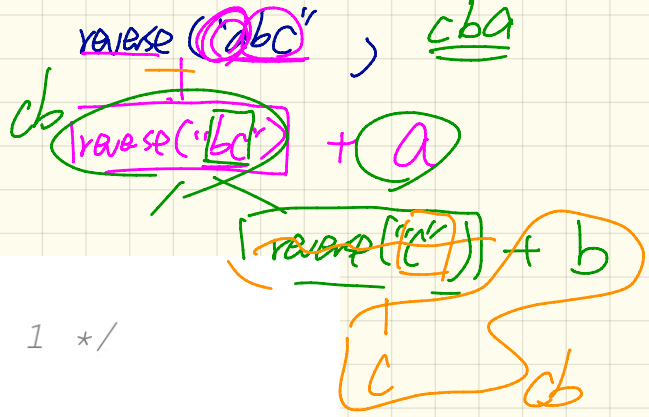
reverse(abcdefgh)

output →

hgfedcba

Reverse of a String

"c"
"bc"
"abc"



```
String reverseOf (String s) {  
  if(s.isEmpty()) { /* base case 1 */  
    return "";  
  }  
  else if(s.length() == 1) { /* base case 2 */  
    return s;  
  }  
  else { /* recursive case */  
    String tail = s.substring(1, s.length());  
    String reverseOfTail = reverseOf(tail);  
    char head = s.charAt(0);  
    return reverseOfTail + head;  
  }  
}
```

tail.length() < s.length()

Number of Occurrences

abca
ooccbca

2
'a'
'd'
0
'c'

"bca"

$$a = a$$
$$0$$
$$1$$

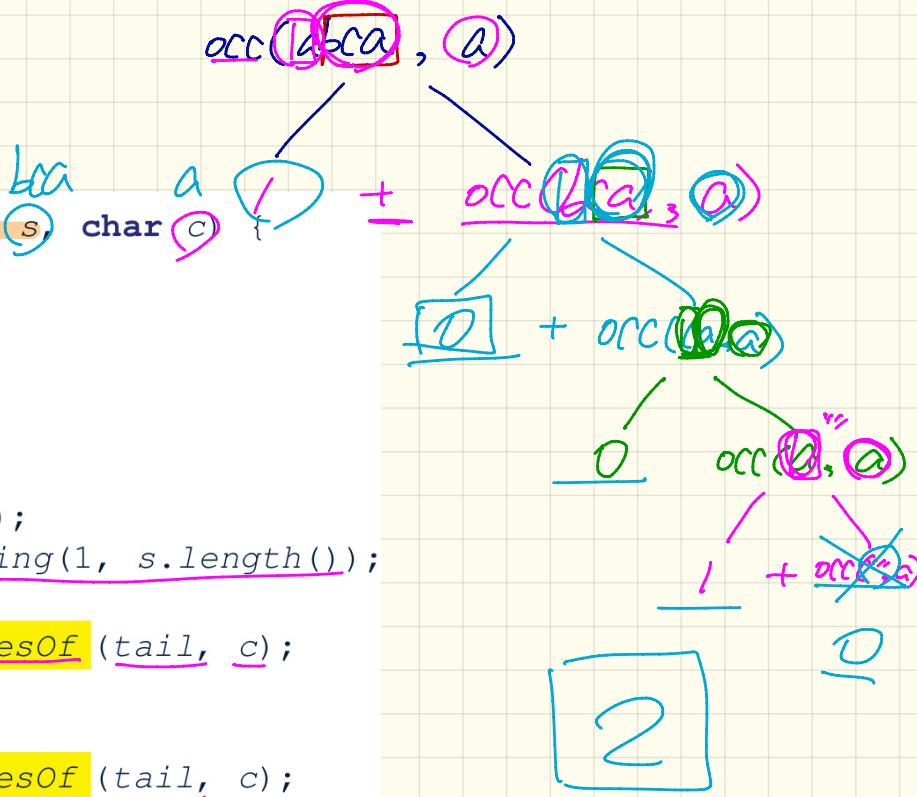
$$\text{occ}(\text{"bca"}, 'a')$$
$$+ 1 = 2$$

$$d = a$$
$$0$$
$$+ \text{occ}(\text{"bca"}, 'd')$$
$$0 = 0$$

$$a = c$$
$$0$$
$$+ \text{occ}(\text{"bca"}, 'c')$$
$$+ 1 = 1$$

Number of Occurrences

```
int occurrencesOf (String s, char c)
{
    if (s.isEmpty()) {
        /* Base Case */
        return 0;
    }
    else {
        /* Recursive Case */
        char head = s.charAt(0);
        String tail = s.substring(1, s.length());
        if (head == c) {
            return 1 + occurrencesOf (tail, c);
        }
        else {
            return 0 + occurrencesOf (tail, c);
        }
    }
}
```



Recursion on Array: Passing a new array

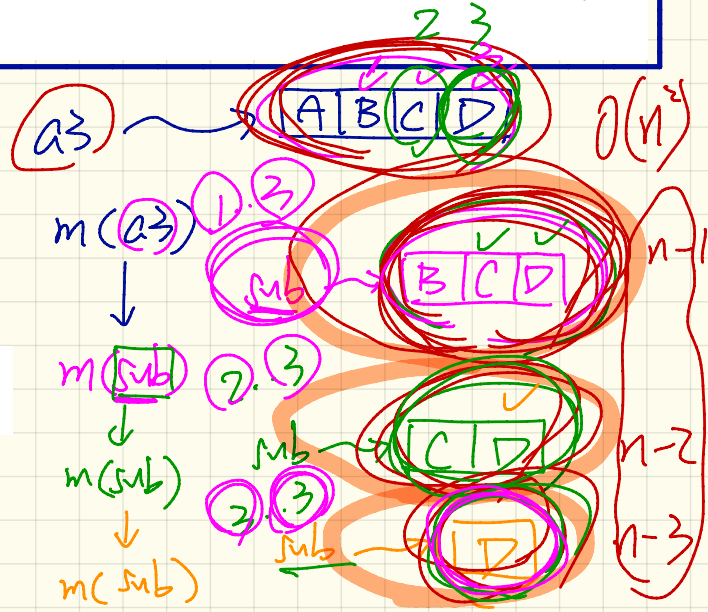
```
void m(int a[]) {  
    if(a.length == 0) { /* base case */ }  
    else if(a.length == 1) { /* base case */ }  
    else {  
        int[] sub = new int[a.length - 1];  
        for(int i = 1; i < a.length; i++) { sub[0] = a[i - 1]; }  
        m(sub) } }  
m(a)
```

strictly smaller than a

Say $a_1 = \{\}$, consider $m(a_1)$ ✓

Say $a_2 = \{A\}$, consider $m(a_2)$ ✓

Say $a_3 = \{A, B, C, D\}$, consider $m(a_3)$



Recursion on Array: Passing an array reference



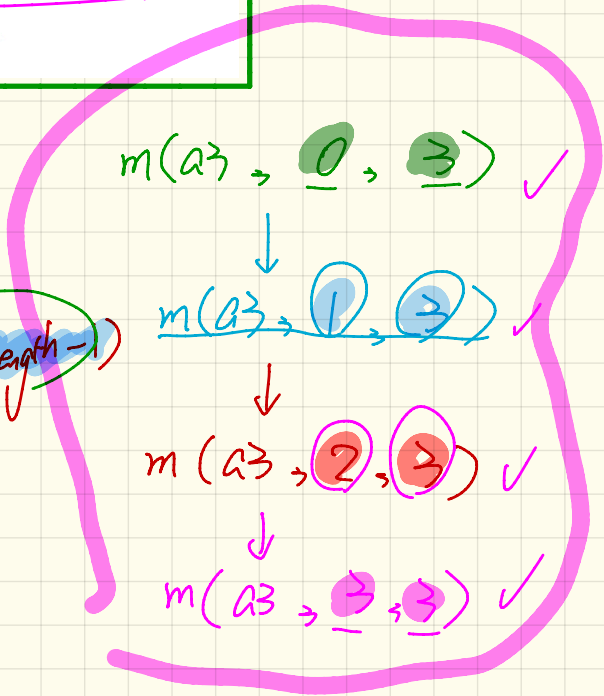
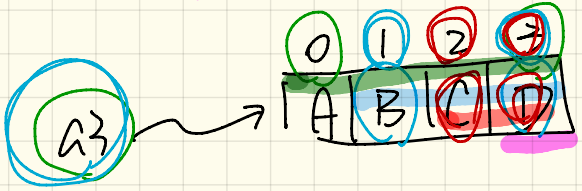
```

void m(int arr[], int from, int to) {
  if (from > to) { /* base case */ }
  else if (from == to) { /* base case */ }
  else { m(arr, from + 1, to) } }
  
```

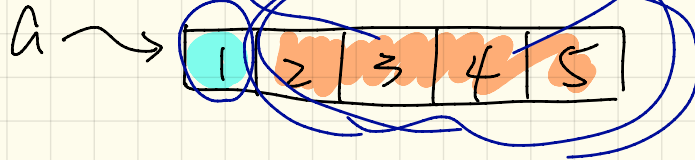
Say $a_1 = \{\}$, consider $m(a_1, 0, a_1.length - 1)$

Say $a_2 = \{A\}$, consider $m(a_2, 0, a_2.length - 1)$

Say $a_3 = \{A, B, C, D\}$, consider $m(a_3, 0, a_3.length - 1)$



allP(a)



$$\text{allP}(a) = a[0] > 0 \quad \&\& \quad \text{allP}([2, 3, 4, 5])$$

└

Are all numbers positive?

allP(a) T



allP(a)
|
allP(a, 0, 2)

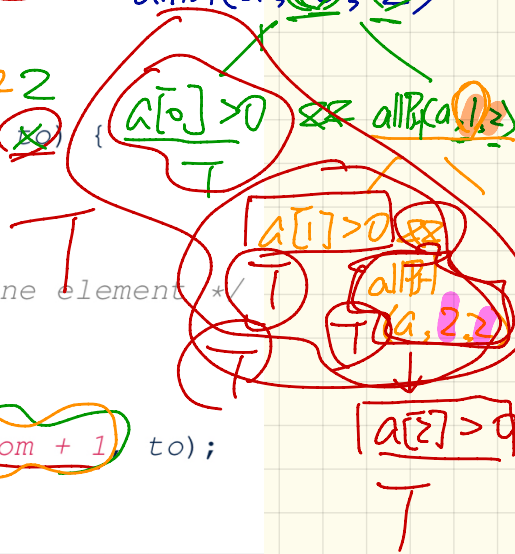
```
boolean allPositive(int[] a) {  
    return allPositiveHelper(a, 0, a.length - 1);  
}
```

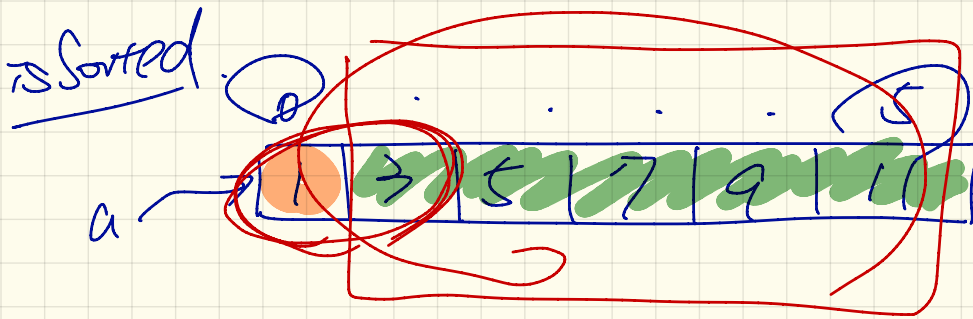
↗ recursive helper method

```
boolean allPositiveHelper(int[] a, int from, int to) {  
    if (from > to) { /* base case 1: empty range */  
        return true;  
    }
```

```
    else if (from == to) { /* base case 2: range of one element */  
        return a[from] > 0;  
    }
```

```
    else { /* recursive case */  
        return a[from] > 0 && allPositiveHelper(a, from + 1, to);  
    }  
}
```





isSorted (a, 0, 5)

= $a[0] \leq a[0+1]$ $\text{isSorted}(a, \underline{0+1}, \underline{5})$